

# Plume Rise and Touchdown during Jack Rabbit Trial 8

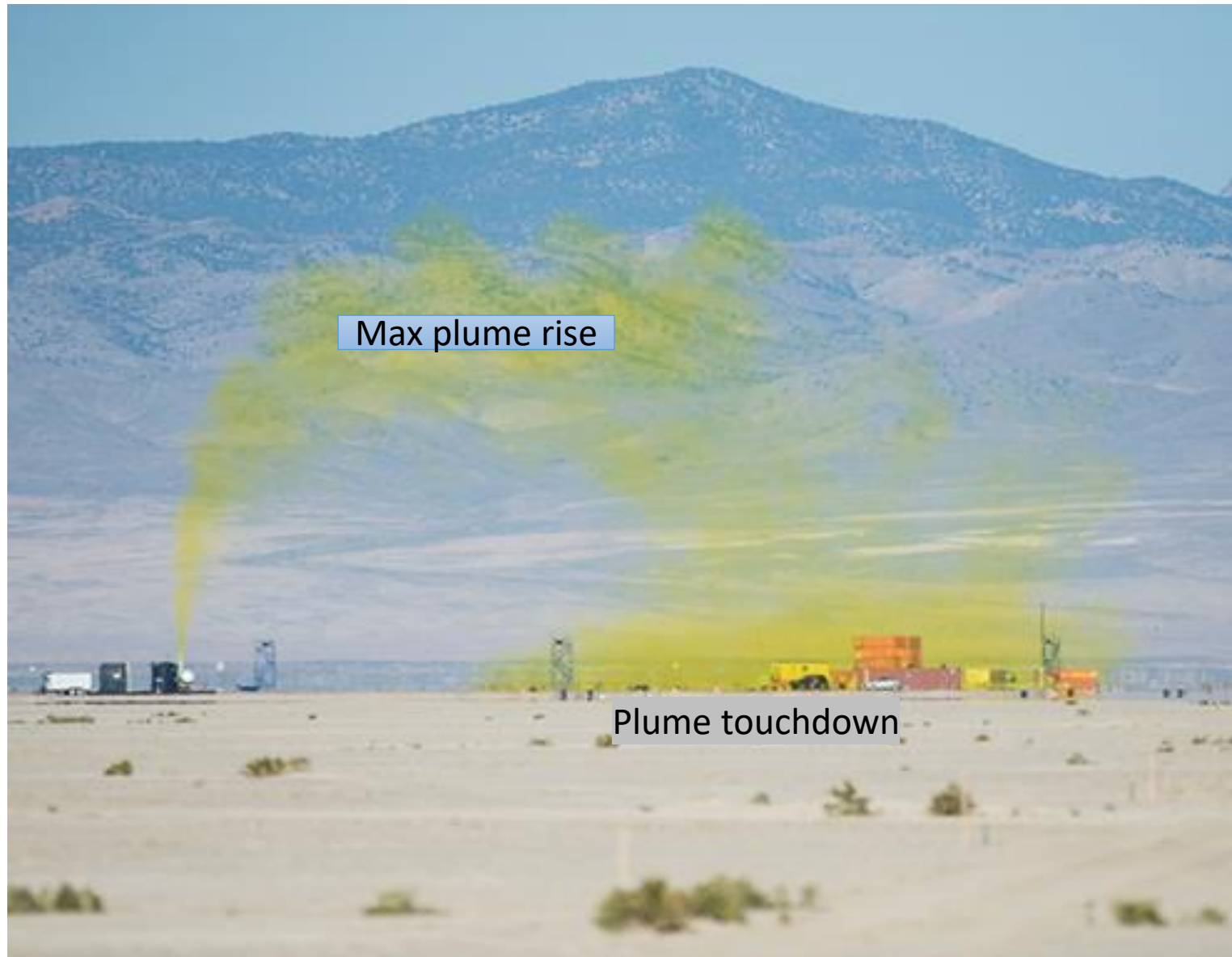
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**Trial 8 dense plume about 30 s after release. Distance from the source to the low red CONEX obstacle is about 85 m**



# Jack Rabbit II 2016

- Sponsored by DHS and DTRA
- 4 trials at DPG, releasing 10 to 20 tons (same set-up as 2015 but with mock urban array removed). Trials 6 and 9 releases were downwards, trial 7 was 45° downwards, trial 8 was vertically up.
- Trial 8 is the only JR(I or II) trial with an upward dense jet release.
- It is also the only vertical dense jet field experiment with releases from a ten ton tank carried out anywhere.
- Can test some models for dense jet: (Briggs, Hoot-Meroney Peterka (HMP) and DRIFT).

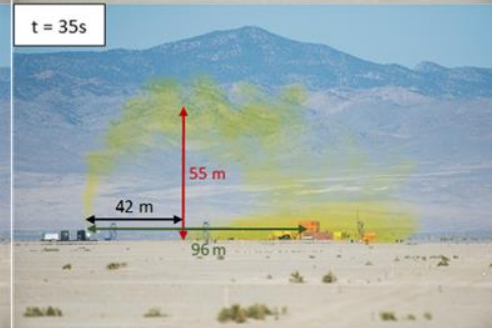
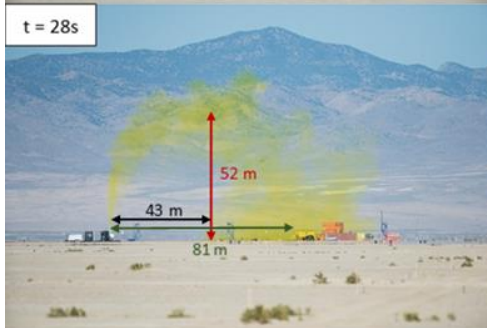
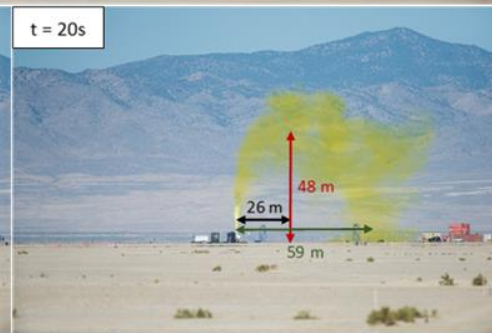
**10 ton Tank used for JR II Chlorine Releases:  
Orange arrow depicts location of hole on top of tank  
(used for Trial 8)**



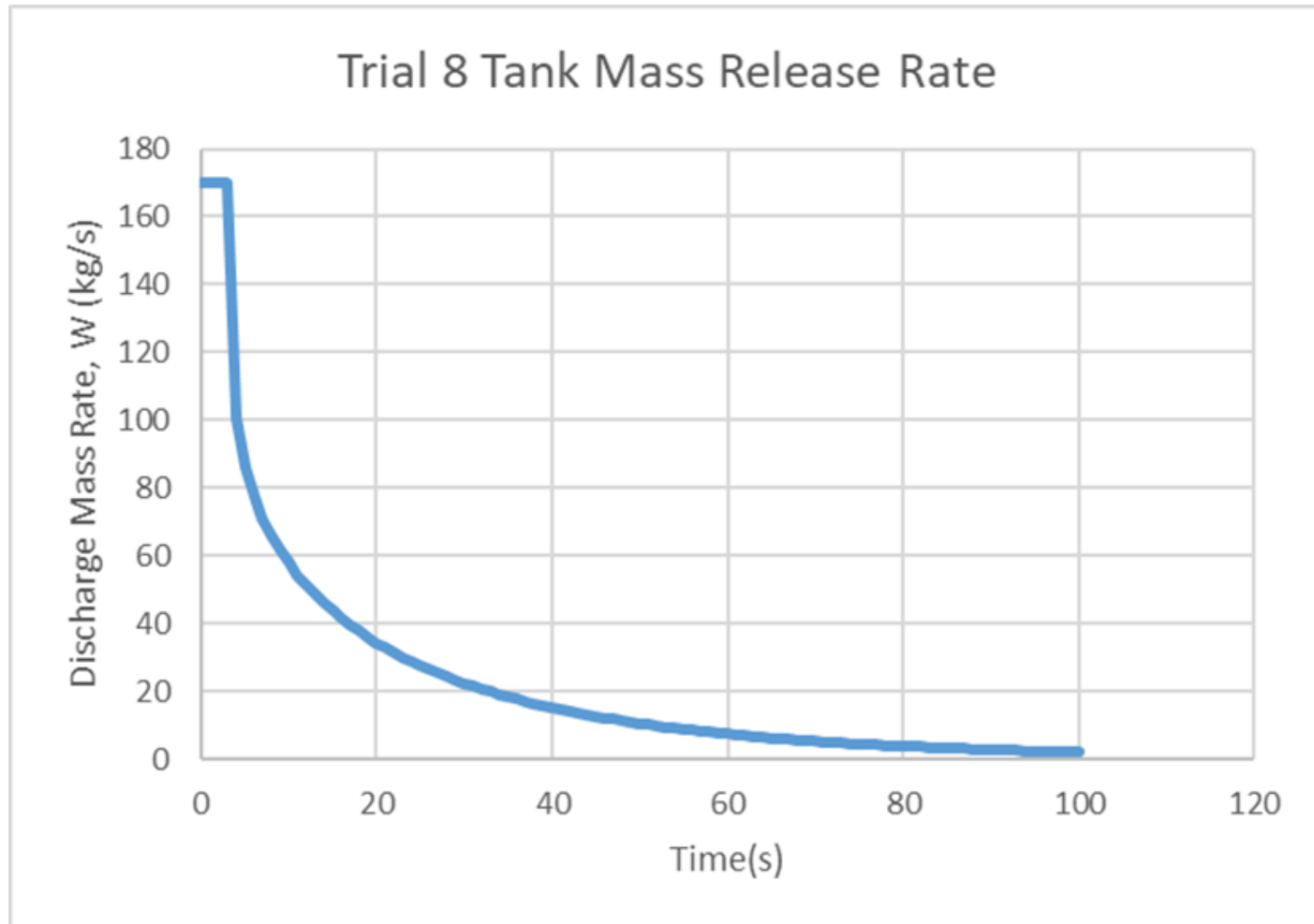
# Trial 8 input conditions

- **Day and time: 9/11/2016 9:01:45 local time**
- **Total jet mass released: 2368 kg**
- **Release duration: 30 s**
- **Average release rate for 30 s duration: 78.9 kg/s**
- **Wind speed at 2 m: 2.2 m/s**
- **Wind direction at 2 m: 175 degrees**
- **Average ambient T: 14.8 C**
- **Stability: Shallow (8 m) well-mixed layer, with inversion above (PG class C at  $z < 8$  m and E at  $z > 8$  m). The Trial 8 jet is within the inversion layer for most of its trajectory.**

Time sequence  
(from 6 to 35 s)  
of Trial 8 plume  
photos



**Mass emission rate decreased with time. For input to models, we assumed 11 time periods (from 0 to 100 s) with constant emissions during each period.**



## **Alternate methods for estimating plume conditions after depressurization (expansion)**

Expansion Model 1. Velocity increases above the exit value due to acceleration by excess pressure at the exit. This is also referred to as a momentum conservation model (e.g., Britter et al., 2011)

Expansion Model 2. Velocity unchanged from exit velocity (e.g., Ewan and Moodie, 1986)



## **Next 5 Slides – Brief descriptions of the three models that were tested**

1. HMP (analytical equations)
2. Briggs (analytical equations)
3. DRIFT (State-of-the art commercial software)

# Hoot, Meroney, and Peterka (1973)

## Plume Rise

HMP analyzed dense plume observations from many experiments in their wind tunnel. Came up with simple analytical formulas based on fundamental science

Plume rise  $\Delta h$  above source:

$$\Delta h/2R_o = 1.32 (w_o/u)^{1/3} (\rho_o/\rho_a)^{1/3} [w_o^2/(2R_o g')]^{1/3}$$

where  $g' = g(\rho_o - \rho_a)/\rho_o$ ;  $g$  is acceleration of gravity,  $\rho_a$  is ambient air density,  $u$  is wind speed, and  $\rho_o$ ,  $R_o$ , and  $w_o$  are initial plume density, radius and vertical velocity after depressurization.

# Hoot, Meroney, and Peterka (1973)

## Touchdown distance

Plume touchdown distance  $x_g$  downwind:

$$x_g/2R_o = w_o u / (2R_o g') + 0.56 \{ (\Delta h / 2R_o)^3 * \\ ((2 + h_s / \Delta h)^3 - 1) u^3 / (2R_o w_o g_a') \}^{1/2}$$

where  $g_a' = g(\rho_o - \rho_a) / \rho_a$  and  $h_s$  is elevation of the stack or vent opening above the ground.

Assumes steady state conditions.

# Briggs 1969 model

For the trajectory of a buoyant (or negatively buoyant) plume as a function of distance,  $x$ , downwind of the release point:

$$\Delta h = [(19(\rho_o/\rho_a)(M_o/u^2)x - 4.2 (B_o/u^3)x^2)]^{1/3}$$

where  $M_o = w_o^2 R_o^2$  is proportional to the initial momentum flux and  $B_o = g[(\rho_o - \rho_a)/\rho_a] w_o R_o^2$  is proportional to the initial buoyancy flux (here assumed positive for a dense cloud). Steady state conditions are assumed.

The maximum rise occurs at the distance where  $d(\Delta h)/dx = 0$ . This equation is most often used for positively buoyant plumes, but is also valid for negatively buoyant clouds.

The plume touchdown distance can be calculated as the distance where  $\Delta h = 0$  (i.e., the first term in the equation equals the second term). That is,  $x_g = 4.52(\rho_o/\rho_a)uM_o/B_o = 4.52 w_o u/[g(\rho_o - \rho_a)/\rho_a]$ . Briggs does not include a formula for maximum ground level concentration,  $C_{\max}$ .

# How is decrease of source emission rate $Q$ with time handled in steady-state HMP and Briggs models?

- 11 piecewise constant  $Q$ 's are determined, fitting the  $Q(t)$  curve in slide 7
- The model solution is calculated for each of the 11  $Q$ 's, assuming steady state conditions

# DRIFT model

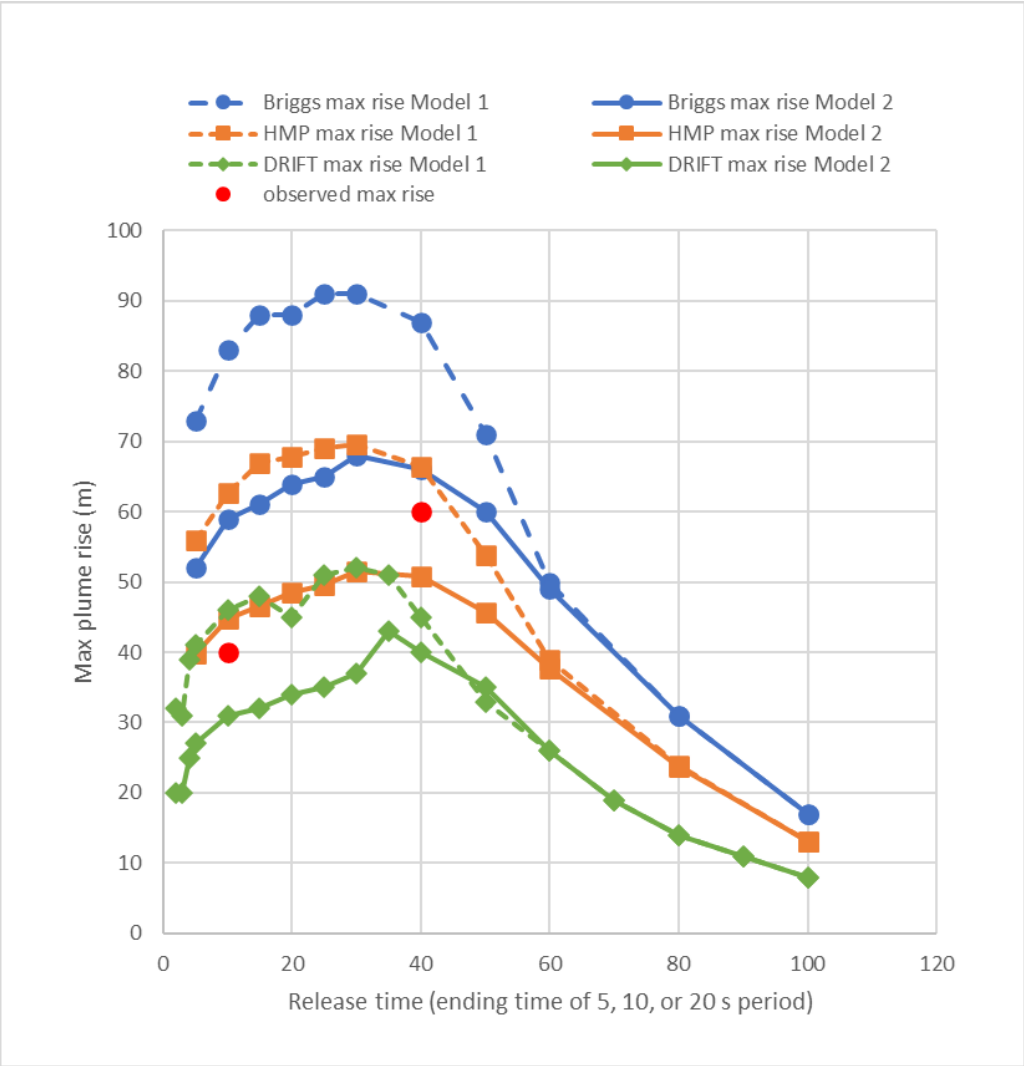
- This is a commercially-available integral dispersion model that is used by HSE for its regulatory work in the UK (Tickle and Carlisle, 2008).
- A momentum-jet model is used to simulate pressurized releases, which includes both single and two-phase jet models, where the latter assumes homogeneous equilibrium between the gas phase and the dispersed liquid droplet phase.
- The thermodynamic models in DRIFT are able to account for multi-component mixtures and humidity effects (condensation and evaporation of water droplets, and associated latent heat transfer), including their effect on cloud buoyancy (Tickle, 2001).
- Releases can be modelled at different angles to the vertical (including the vertically-upwards case in Trial 8) and also for different lateral cross-wind directions.

# Results of comparisons of the three models are given below

- Maximum plume rise
- Touchdown distance
- Ground level concentration at touchdown
  
- Calculations are made for 11 piecewise emission periods that match the decrease of  $Q$  with time in slide 7

# Observed and modeled maximum vertical plume rise, calculated using emissions rates for 11 time segments after release was initiated.

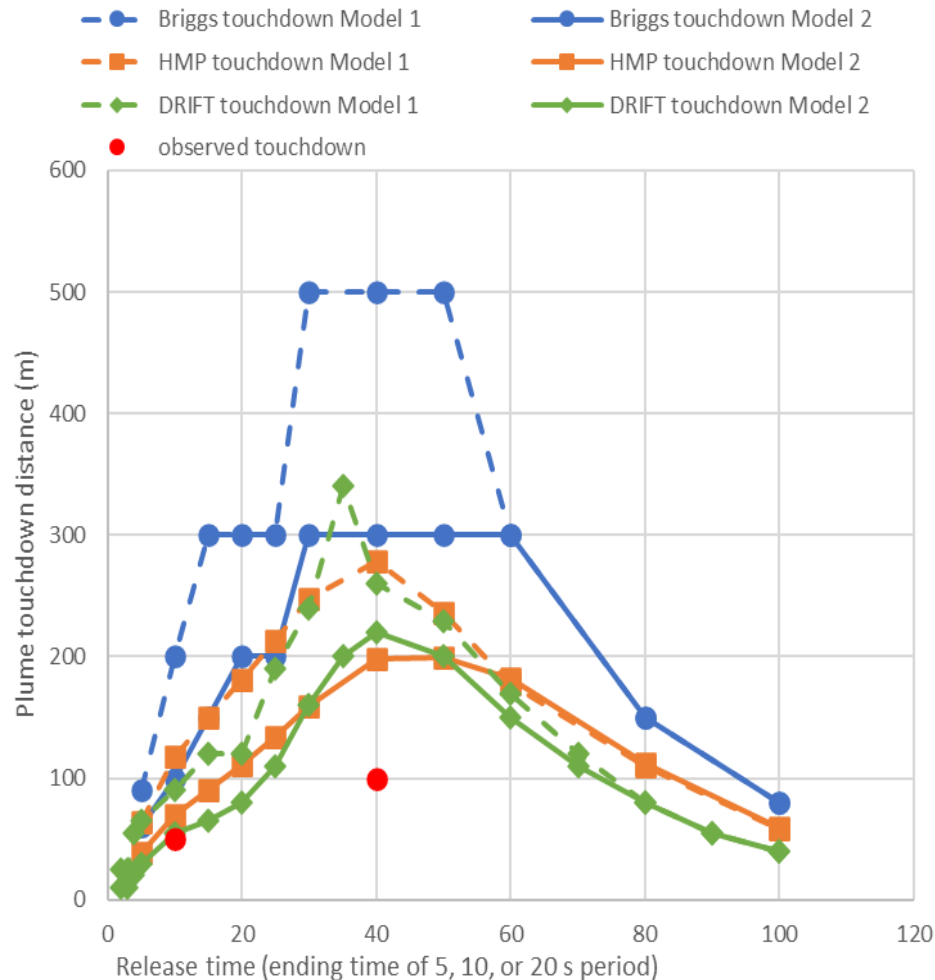
The two red dots are observations





# Observed and modeled distance to plume touchdown, calculated using emissions rates for 11 time segments after release was initiated.

The two red dots are observations



## Comparison of observed and modeled maximum concentration. Model predictions are at touchdown distance

	Observed at 85 m	HMP Model 1	HMP Model 2	DRIFT Model 1	DRIFT Model 2
Maximum C (ppm)	12080	9570	17660	6600	14000

# Conclusions

- The predictions of three dense jet models (HMP, Briggs, and DRIFT) were compared to the observed initial plume rise, touchdown distance, and maximum ground level concentrations during Trial 8 of JR II.
- Predictions of the three models were shown to usually agree with the observed heights and distances within about a factor of two.
- The Briggs model predictions of the distance to maximum plume rise and touchdown were about a factor of two to five too large.
- Additionally, the HMP and DRIFT models predicted chlorine concentrations near the plume touchdown position within a factor of two of the observations.

# Acknowledgements

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